

Example

A cylinder has internal diameter of 1m and its walls are 1.5cm thick. This cylinder is 1.5m long. Find out change in volume if a fluid under 15 kg/cm^2 pressure is introduced into it. $E = 2 \times 10^6 \text{ kg/cm}^2$; poisson's ratio $= 0.3$.

Solution

Radius of cylinder $r = \frac{1}{2} \text{ m} = 50 \text{ cm}$; wall thickness $t = 1.5 \text{ cm}$

Length of cylinder $L = 1.5 \text{ m} = 150 \text{ cm}$; fluid pressure $p = 15 \text{ kg/cm}^2$

Volume of cylinder $= \pi r^2 L$

$$= \pi \cdot 50^2 \cdot 150 = 11.781 \times 10^5 \text{ cm}^3$$

$$\text{Volumetric strain } e_v = \frac{pr}{tE} \left(\frac{5}{2} - \frac{2}{m} \right)$$

$$= \frac{15 \times 50}{1.5 \cdot 2 \times 10^6} \left(\frac{5}{2} - 2 \cdot 0.3 \right)$$

$$= 0.475 \times 10^{-3}$$

$$\therefore \text{Change in Volume } \Delta V = e_v \cdot V = 0.475 \times 10^{-3} \cdot 11.781 \times 10^5$$

$$= \underline{559.6 \text{ cm}^3}$$

Example

A thin cylindrical shell with the following dimensions has been filled with a liquid at atmospheric pressure: Length = 1.2m, External diameter = 20 cm. Thickness of metal = 8 mm.

Assuming values of Modulus of elasticity E and Poisson's ratio μ as $21 \times 10^6 \text{ kg/cm}^2$ and 0.33 respectively, find the value of pressure exerted by the fluid on the wall of the cylinder and the hoop stress induced if an additional 25 cm^3 of the ~~the~~ liquid is pumped into the cylinder.

Solution

Inner radius of shell $r = \frac{20 - 20 \times 0.8}{2} = 9.2 \text{ cm}$

Change in volume $\delta V = 25 \text{ cm}^3$

Original volume of shell $V = \pi r^2 \cdot l$
 $= \pi \cdot 9.2^2 \cdot 120 = 31908.5 \text{ cm}^3$

Volumetric strain $e_v = \frac{\delta V}{V} = \frac{25}{31908.5} = 0.0007834$

If e_h and e_l are the hoop strain and longitudinal strain resp., then we have:

$$e_v = \frac{pr}{tE} \left(\frac{5}{2} - \frac{2}{m} \right) = \frac{p \cdot 9.2}{0.8 \cdot 21 \times 10^6} \left(\frac{5}{2} - 2 \cdot 0.33 \right) = 0.0007834$$

$\therefore$ fluid pressure is $p = \underline{77.75 \text{ kg/cm}^2}$

Hoop stress $p_h = \frac{pr}{t} = \frac{77.75 \cdot 9.2}{0.8} = \underline{894.125 \text{ kg/cm}^2}$