EEE 3352

Electromechanics & Electrical Machines



Lecture 8: Three phase AC machines

Dr A Zulu © 2023



8. Three-Phase AC Machines

- 1. Production of rotating magnetic field
- 2. Induction machine
- 3. Synchronous machine

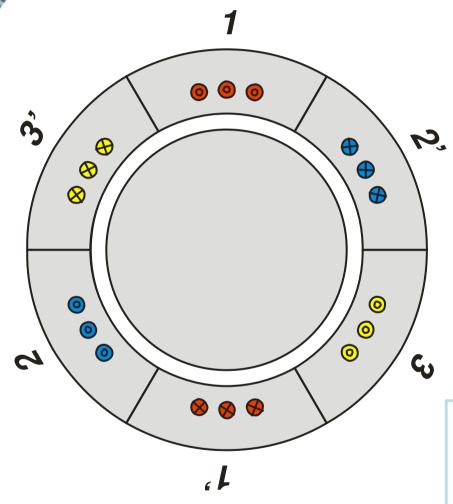


Objectives:

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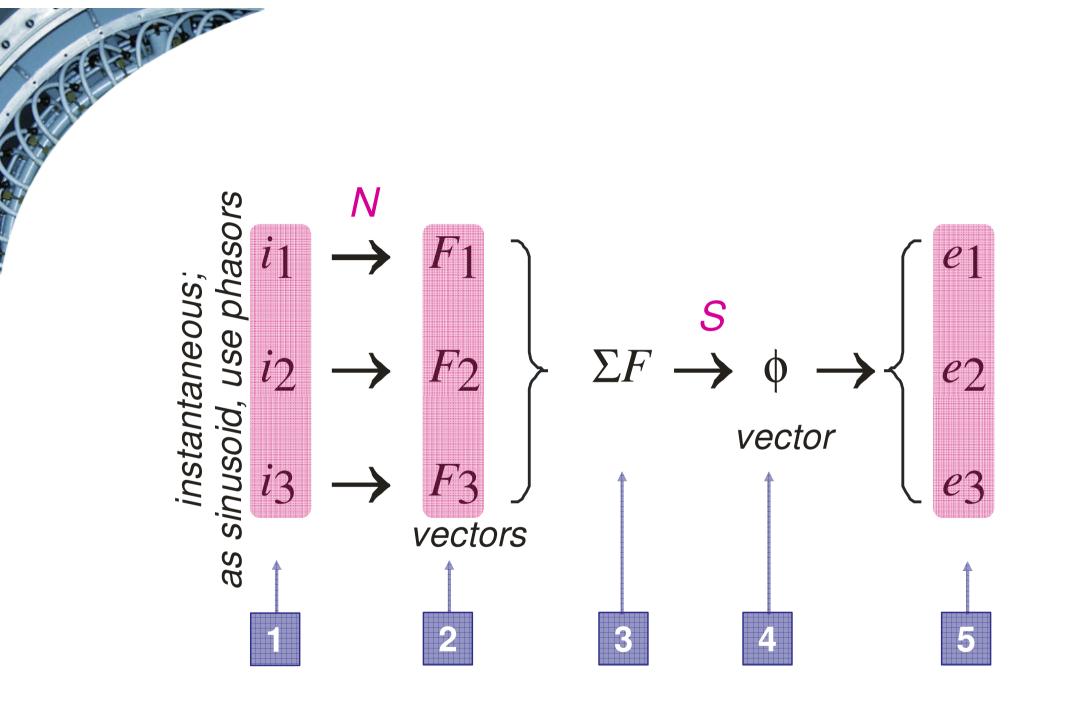
- at the end of the lecture, students should be able to
 - show the process for producing a rotating magnetic flux from three phase currents
 - explain the principle of operation of the three phase induction motor
 - determine the proportions of distribution of power in the elements of the induction motor
 - explain the principle of operation of the synchronous machine
 - differentiate the different modes of operation of the synchronous machine

8.1. Rotating magnetic field



- balanced 3-phase supply
- 3 identical coils 120° from each other
- each coil has N -turns





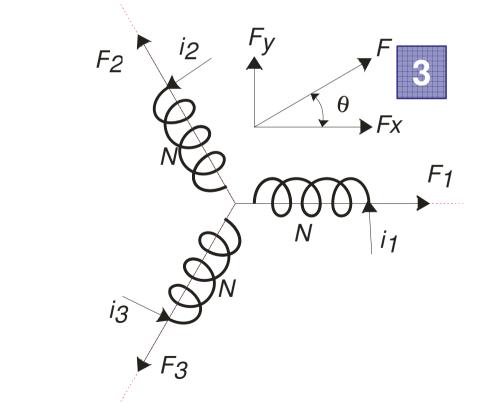
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• let

$$i_{1} = I_{m} \cos \omega t$$
$$i_{2} = I_{m} \cos(\omega t - 120^{\circ})$$
$$i_{3} = I_{m} \cos(\omega t + 120^{\circ})$$

 $F_{1} = NI_{m} \cos \omega t$ $F_{2} = NI_{m} \cos(\omega t - 120^{\circ})$ $F_{3} = NI_{m} \cos(\omega t + 120^{\circ})$





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$$F_{x} = F_{1} - \frac{1}{2}(F_{2} + F_{3})$$

$$= NI_{m} \left[\cos \omega t - \frac{1}{2} \left\{ \cos(\omega t - 120^{\circ}) + \cos(\omega t + 120^{\circ}) \right\} \right]$$

$$= NI_{m} \left[\cos \omega t - \frac{1}{2} 2 \cos \omega t \cos 120^{\circ} \right]$$

$$F_{x} = \frac{3}{2} NI_{m} \cos \omega t$$



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$$F_{y} = \frac{\sqrt{3}}{2} (F_{2} - F_{3})$$

$$= \frac{\sqrt{3}}{2} NI_{m} \Big[\cos(\omega t - 120^{\circ}) - \cos(\omega t + 120^{\circ}) \Big]$$

$$= \frac{\sqrt{3}}{2} NI_{m} 2 \sin \omega t \sin 120^{\circ}$$

$$F_{y} = \frac{3}{2} NI_{m} \sin \omega t$$

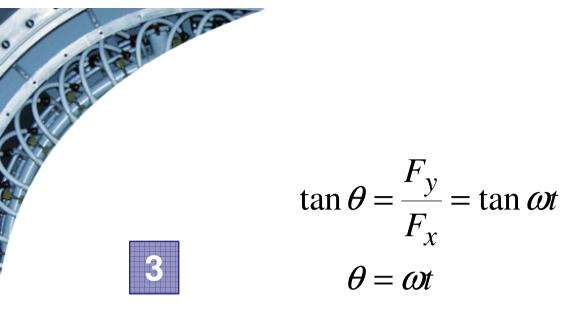




$$|F| = \sqrt{F_x^2 + F_y^2} = \frac{3}{2}NI_m$$

- magnitude of the resultant mmf in space is
 - independent of time
 - constant





- direction of the resultant mmf in space
 - 1) varies continuously in time
 - 2) varies at angular speed ω

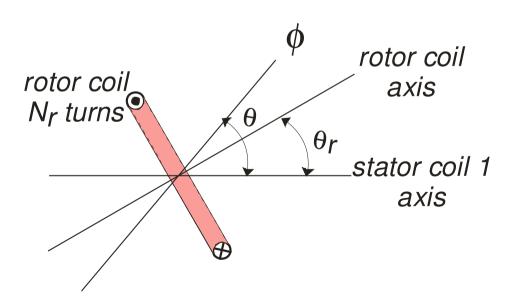




Ζ,

$$\varphi = \frac{F}{S} = \frac{3}{2} \frac{NI_m}{S}$$

- reluctance S, though difficult to evaluate, is at least constant
- *p* has constant value and rotates in space at constant speed



$$\theta = \omega t$$
$$\theta_r = \omega_r t + \beta$$



• flux linking rotor coil *r* is

$$\phi_r = \phi \cos(\theta - \theta_r) = \phi \cos\left[(\omega - \omega_r t) - \beta\right]$$

• define slip, s

$$s = \frac{\omega - \omega_r}{\omega}$$

• then

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$$\phi_r = \phi \cos[s\omega t - \beta]$$

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• induced voltage in rotor, e_r , using Faraday's Law

$$e_r = N_r \frac{d\phi_r}{dt}$$

= $N_r \phi [\sin \{s\omega t - \beta\}] s\omega$
 $e_r = sN_r \phi \omega \sin(s\omega t - \beta)$

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induced voltage in rotor coil has

- amplitude \propto **s**
- frequency \propto **s**
- 2 special cases:

NO ATA

- 1) at synchronous speed, s = 0
 - $e_r = 0$: synchronous machine

2) at standstill, s = 1

$$e_r = N_r \phi \omega \sin(\omega t - \beta)$$
 : transformer

voltages in stator & rotor windings

• for stator coil 1

$$e_1 = N \frac{d(\phi \cos \theta)}{dt} = -N \phi \omega \sin \omega t$$

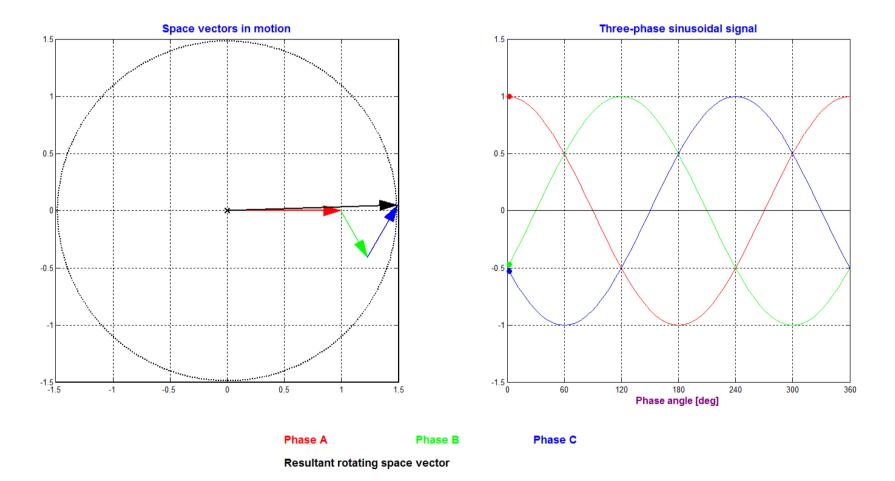
rms values

$$E_r = s \frac{N_r}{\sqrt{2}} \phi \omega$$
$$E_1 = \frac{N}{\sqrt{2}} \phi \omega$$

$$\frac{E_r}{E_1} = s \frac{N_r}{N}$$



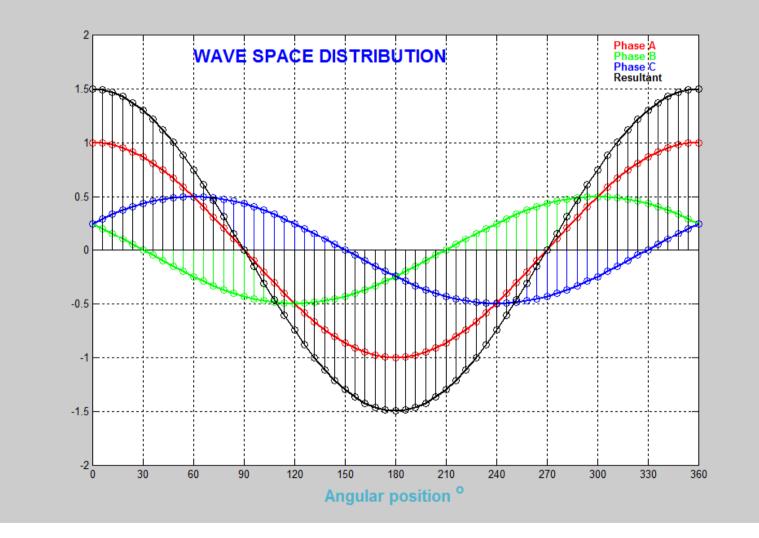
3-phase sinusoidal currents and their mmf wave vectors



Credits: http://www.ece.umn.edu/users/riaz/animations/listanimations.html

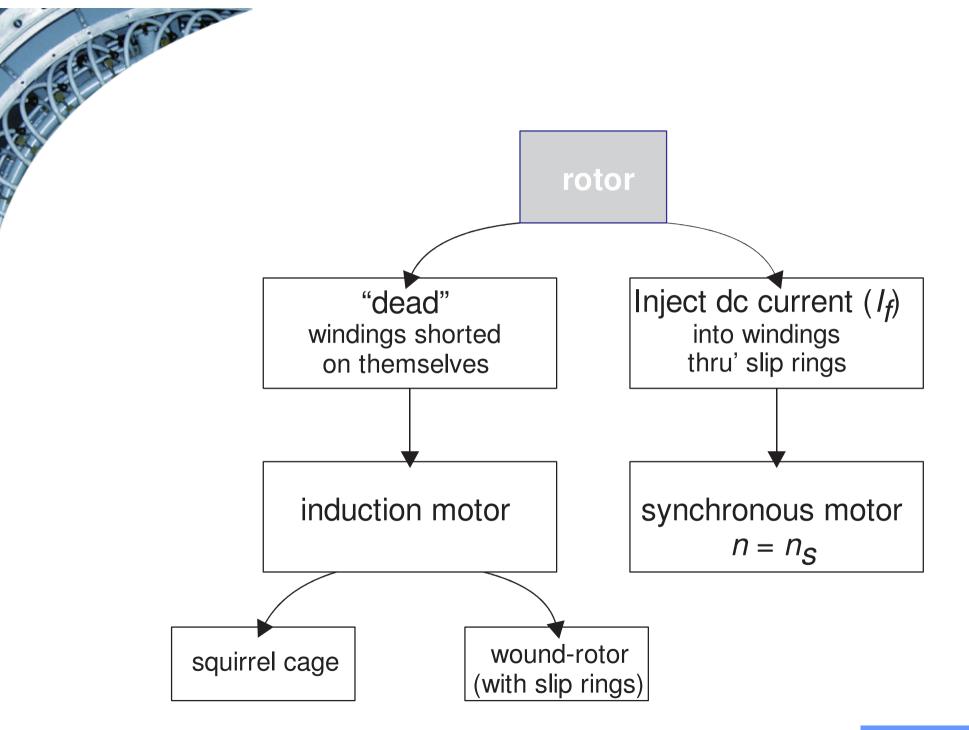


Travelling wave F or ϕ caused by 3-phase sinusoidal currents



Credits: http://www.ece.umn.edu/users/riaz/animations/listanimations.html





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8.2 Induction machines

Stator

Smooth yoke











Rotor

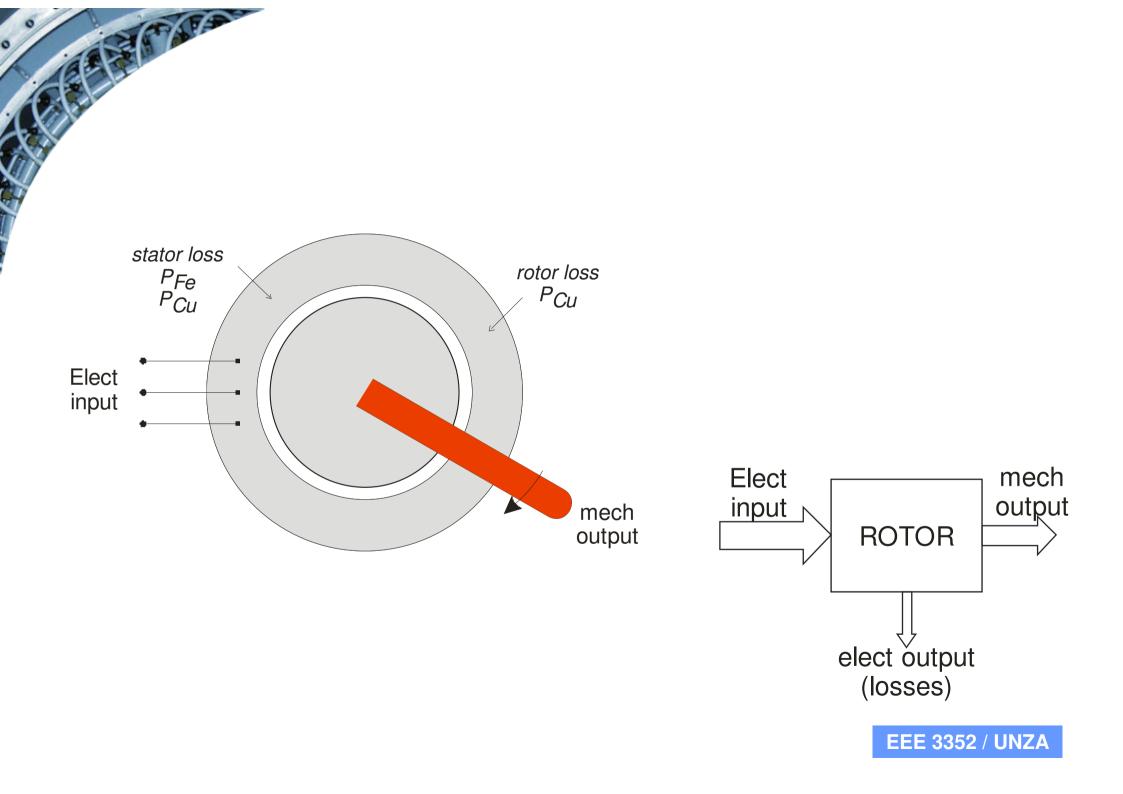
Squirrel cage

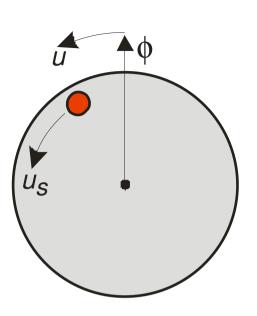
Wound rotor / Slip ring











- single conductor of length /
- carrying current *i*
- at radius *R*
- rotating magnetic field is moving at speed *u*
- conductor is moving at speed u_r

• define (fractional) slip s as

$$s = \frac{u - u_r}{u}$$

• hence

2 CT STA

$$s = \frac{2\pi Rn - 2\pi Rn_r}{2\pi Rn} = \frac{n - n_r}{n}$$

• Faraday's law gives induced voltage

$$V_{in} = Bl(u - u_r) = Blus$$



• rotor electrical power: $e_r i = (Blus)i$

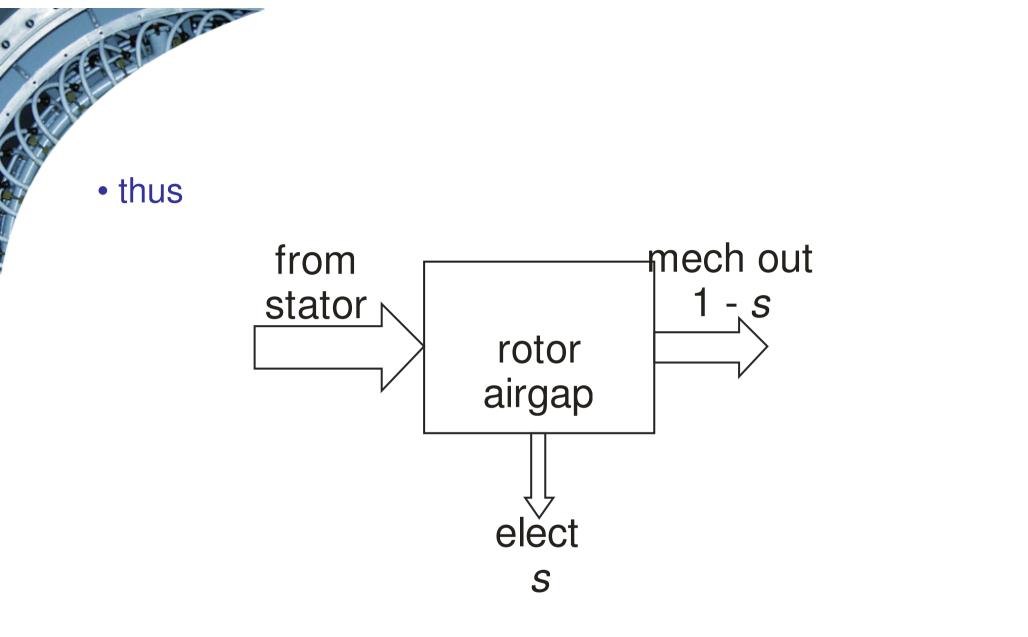
• mech force: Bli

DE CONTA

- mech power: $(Bli)u_r = Bliu(1-s)$
- total input power: rotor elec power + rotor mech power

$$= Blusi + Bliu(1-s)$$
$$= Blui$$







- designer ensures that s is small
- typical values

A STATA

- small motor (few kW) **s** = 0.03 (3%)
- large machines $S \le 0.02$

Examples

- 1) A 4-pole 50-Hz machine is running at s = 0.025 and 100 kW enters the rotor. What is the speed *n*, mechanical output and the rotor copper loss?
- A 3-phase, 60-Hz, four-pole, 220-V, wound-rotor induction motor has a delta-connected stator winding and a star-connected rotor winding. The rotor has 40% as many turns as the stator. For a rotor speed of 1710 r/min, calculate the
 - a) slip

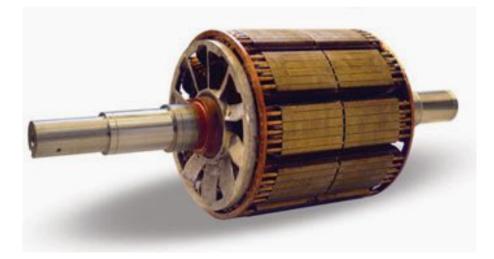
A CONTA

- b) induced phase voltage in the rotor at standstill
- c) induced phase voltage in the rotor at working speed
- d) rotor terminal voltage on open circuit and at standstill
- e) frequency of induced voltage in the rotor

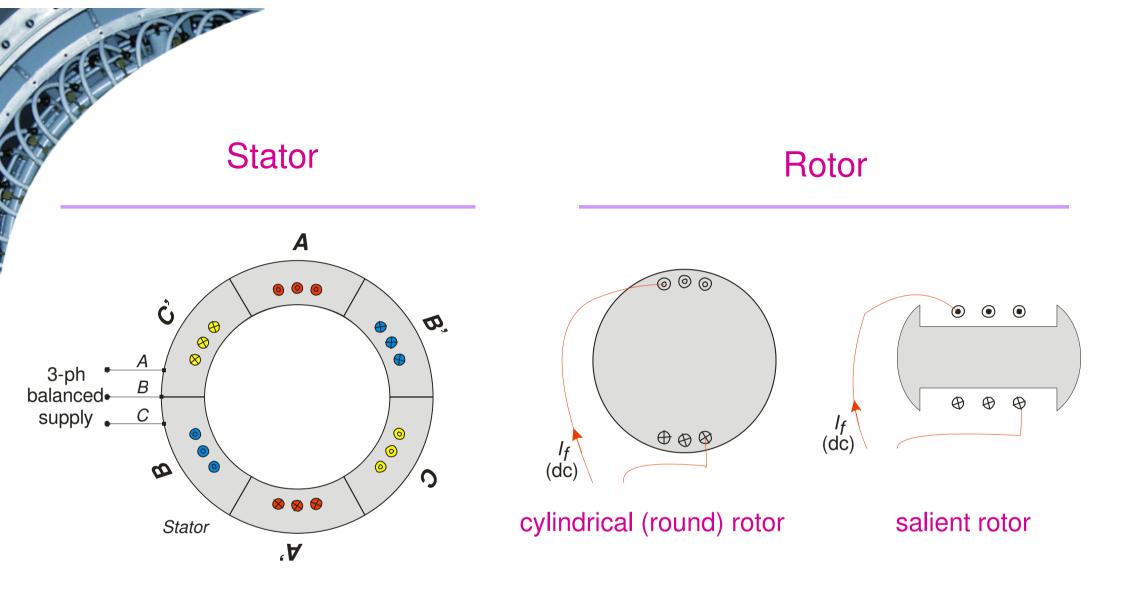
8.3 Synchronous machines

- the synchronous machine has
 - a 3-phase winding on the stator
 - a rotor supplied with direct current

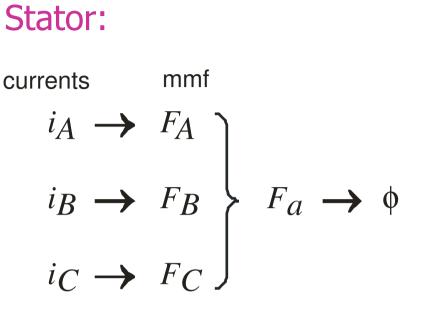








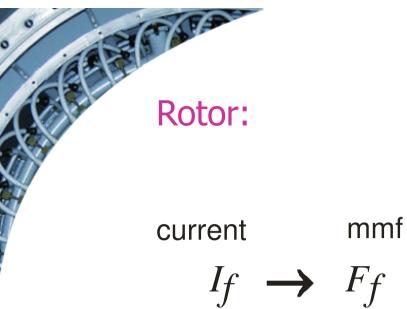
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- F_a has constant magnitude and rotates a constant speed ω
- for a 2p-pole machine

$$n = \frac{\omega}{2\pi} = \frac{f}{p}$$



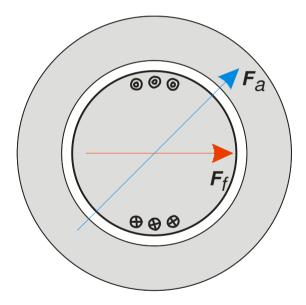


- direction of the current through the brushes and slip rings to the winding is always in the same direction
- polarity on the rotor (N & S) never changes
- F_f is along the axis of the rotor and rotates at ω_r



$$\overline{F}_{a} + \overline{F}_{f} = \overline{F}_{r} \rightarrow \phi_{r} \rightarrow \begin{cases} e_{A} \\ e_{B} \\ e_{C} \end{cases} E_{r}$$

• in synchronous machine $\omega_r = \omega$



 the machine functions as a motor or as a generator depending on whether the stator (armature) field leads or lags the rotor field 8.3.1 Action of the ideal machine

• assume:

- ideal cylindrical rotor
- connected to 'infinite' busbar
- stator windings have
 - negligible resistance
 - negligible leakage reactance
 - uniform air gap
 - high permeability magnetic circuit
 - no saturation
 - balanced load



- to work at all, the rotor must rotate at synchronous speed
- no torque can be developed if rotor is unexcited
- stator must draw lagging reactive power

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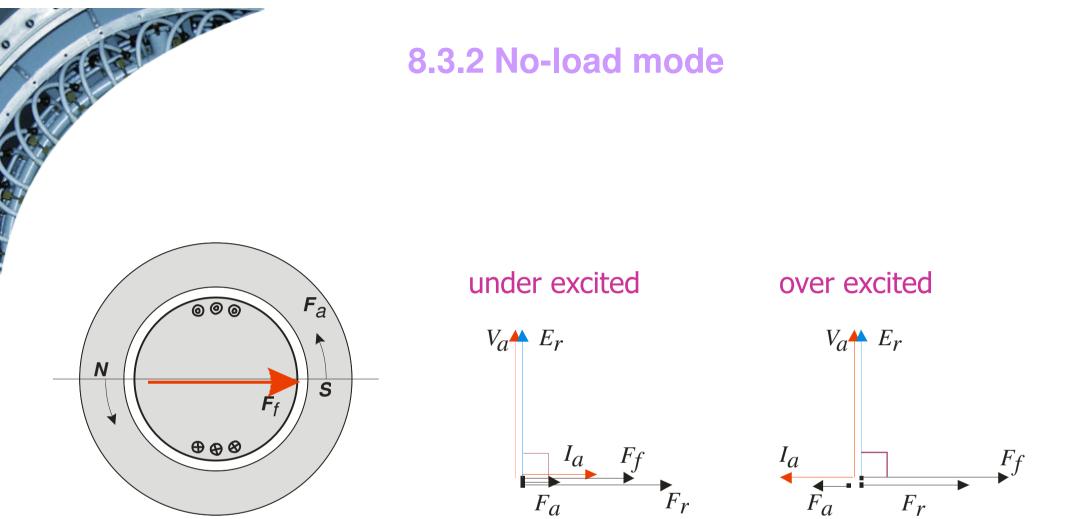
- to magnetise the machine to a gap flux per pole of ϕ_r (resultant)
 - in order for the stator emf E_r (r = resultant) to be induced
 - to balance applied voltage V_a (v_1 , v_2 , v_3)

- if rotor is given a small dc excitation
 - it takes over part of the task of exciting the magnetic circuit,
 - reducing the demand of stator magnetising power
 - i.e. under excitation
 - λ = torque angle
 - δ = load angle

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- motor mode: δ is negative
- generator mode: δ is positive

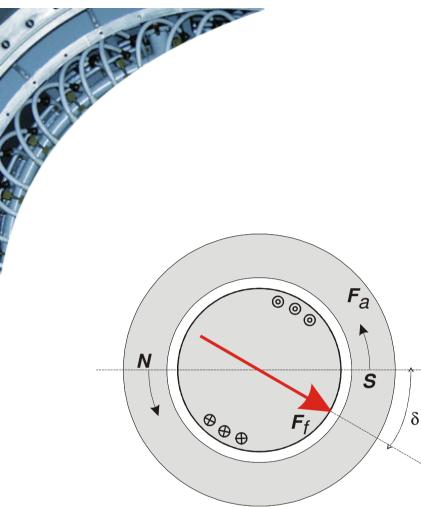




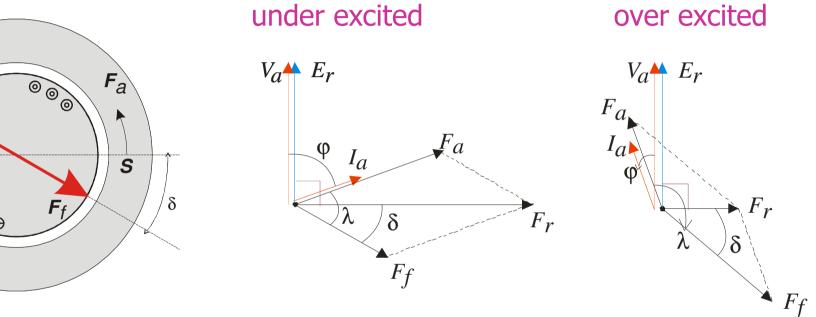
• no torque is developed

DE CAPA

- mmf axes are in alignment, torque angle is zero
- F_a and F_f combine to give F_r necessary to produce ϕ_r
- if rotor mmf is increased very much into over excitation
 - the stator must produce a demagnetising current so that F_r shall remain unchanged
 - i.e. stator must produce a leading current



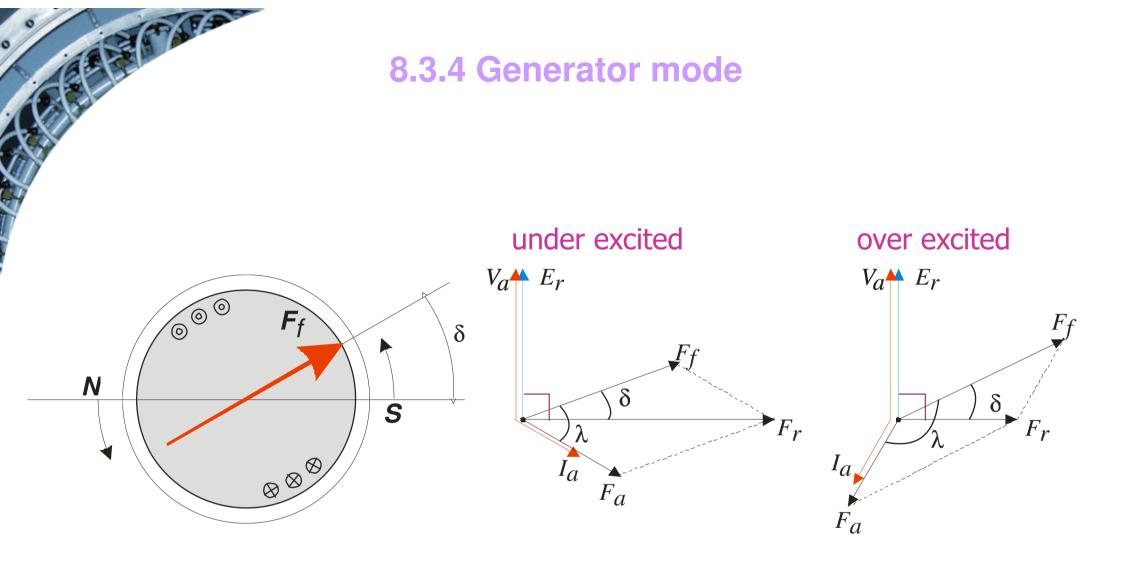
8.3.3 Motor mode



- depending on whether rotor is under or over excited
 - stator takes an active current component
 - accepting power from the supply and
 - developing a forward torque on the rotor
 - to balance the load torque
- the reactive component of the current, as on no-load,
 - compensates for under or over excitation

 $T \propto \sin \lambda$







- the active component of stator current reverses
 - thus delivering power into the supply
 - developing a counter torque on the rotor
 - to balance the driving torque
- the reactive component of the current, as on no-load,
 - compensates for under or over excitation

8.3.5 Compensator mode

- a synchronous machine designed
 - to run unloaded
 - the shaft is not connected to mechanical load or prime mover
- variation of rotor excitation causes machine to take purely reactive power
 - under excitation \rightarrow lagging
 - over excitation \rightarrow leading

application is in

SPATATA

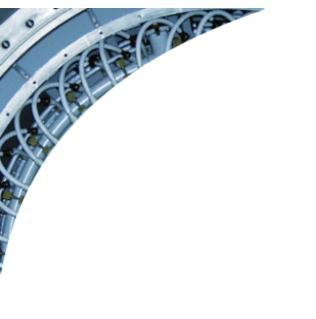
- control of voltage of transmission systems by
 - supplying reactive power
 - consuming reactive power
- a.k.a. synchronous compensator, synchronous capacitor
- in general, the machine has no torque at starting (zero speed)
 - some other means must be used to bring it to synchronous speed, e.g.
 - pony motor
 - double-cage arrangement



8.3.6 Starting of synchronous motor

- in general, the machine (motor, compensator) has no torque at starting (zero speed)
 - some other means must be used to bring it to synchronous speed, e.g.
 - pony motor
 - double-cage arrangement
 - cage 1: induction machine
 - cage 2: synchronous machine





- End of Lecture 8 -

