

## EEE 3352: Electromechanics & Electrical Machines

ASSIGNMENT 1: ELECTROMAGNETIC FIELDS (Class Quiz - xx/07/2021) Time 80 minutes

1. *Two circular metal plates of diameter 20 cm are placed equidistant in air at 4 mm from each other and are subjected to 600 V dc between them.* What is the capacitance created by the plates in uF? [1 decimal place] [5]

$$C = \frac{\varepsilon A}{l} = \frac{\varepsilon_r \varepsilon_0 A}{l} = 6.95 \times 10^{-7} \text{ F}$$
  
Ans: 69.5 µF

2. *Two circular metal plates of diameter 20 cm are placed equidistant in air at 4 mm from each other and are subjected to 600 V dc between them.* What is the electric field strength, in V/mm, at the centre of the plates and mid-way between the plates? [A whole number, 0 decimal places] [5]

$$E = \frac{V}{l} = 2.50 \times 10^5$$
 V/m

Ans: 250 V/mm

3. *Two circular metal plates of diameter 20 cm are placed equidistant in air at 4 mm from each other and are subjected to 600 V dc between them.* What is the electric field strength, in V/mm, at the centre of the plates and three-quarter distance from the postive plate? [A whole number, 0 decimal places] [5]

$$E = \frac{V}{l} = 2.50 \times 10^5 \text{ V/m}$$
  
Ans: 250 V/mm

4. Two circular metal plates of diameter 20 cm are placed equidistant in air at 4 mm from each other and are subjected to 600 V dc between them. What is the energy density, in  $J/m^3$ , at the centre of the plates and threequarter distance from the postive plate? [2 decimal place] [5]

$$W_{density} = \frac{1}{2}DE = \frac{1}{2}\varepsilon E^2 = 0.28 \text{ J/m}^3$$
  
Ans: 0.28 J/m<sup>3</sup>

5. *Two circular metal plates of diameter 20 cm are placed equidistant in air at 4 mm from each other and are subjected to 600 V dc between them.* What is the force, in mN, on the postive plate? [1 decimal place] [5]

*Force* = 
$$\frac{1}{2}DEA = \frac{1}{2}\varepsilon E^2 A = 8.7 \times 10^{-3} N$$
  
Ans: 8.7 mN

6. A 100-m concentric cable has a central copper conductor and a metallic metal covering embracing diameters of 1 cm and 3 cm, respectively. If the electric field strength capability of the of the insulation is 2 kV/mm, what is the maximum dc voltage, in kV, that can be applied to the cable? [1 decimal place] [7.5]

$$E_{\max} = \frac{V}{r_1 \ln \frac{r_2}{r_1}} \rightarrow V = r_1 \ln \frac{r_2}{r_1} E_{\max} = 1099 \text{ V}$$
  
Ans: 1.1 V

7. A 100-m concentric cable has a central copper conductor and a metallic metal covering embracing diameters of 1 cm and 3 cm, respectively. If the relative permittivity of the insulation of the cable is 4.5, what is the capaciatance, in nF, of the cable? [1 decimal place] [5]

$$C = \frac{2\pi l \varepsilon_r \varepsilon_0}{\ln \frac{r_2}{r_l}} = 2.28 \times 10^{-8} \text{ F}$$
  
Ans: 22.8 nF

8. *A 100-m concentric cable has a central copper conductor and a metallic metal covering embracing diameters of 1 cm and 3 cm, respectively.* If the relative permittivity of the insulation of the cable is 4.5 and 1 kV is applied, what is the electric field strength, in V/mm, at a point mid-way between the radius of copper conductor and the metallic sheath? [A whole number, 0 decimal places] [10]

$$r_m = r_1 + \frac{r_2 - r_1}{2} = \frac{r_1 + r_2}{2}$$
$$E(r_m) = \frac{V}{\ln \frac{r_2}{r_1}} \frac{1}{r_m} = 246630 \text{ V/m}$$

9. A 100-m concentric cable has a central copper conductor and a metallic metal covering embracing diameters of 1 cm and 3 cm, respectively. What is the resistance of the insulation, in G $\Omega$ , if the conductivity of the insulation is 10<sup>-14</sup> S/m? [A whole number, 0 decimal places] [10]

$$R_{Cu} = \frac{l}{\sigma A} = \frac{l}{\sigma (\pi r_1^2)} = 0.0216 \,\Omega$$
  
Ans: 21.6 mΩ

10. A 100-m concentric cable has a central copper conductor and a metallic metal covering embracing diameters of 1 cm and 3 cm, respectively. If the conductivity of copper is 59 MS/m, what is resistance of the cable, in m $\Omega$ , over its run? [1 decimal place] [10]

$$R_{ins} = \frac{1}{G_{ins}} = \frac{\ln \frac{r_2}{r_1}}{2\pi l\sigma} = 175 \times 10^9 \ \Omega$$
Ans: 175  $\Omega$ 

11. A toroid made of steel of relative permeability of 1800 is wound with a coil of 100-turns, carrying a current of 1 A dc. If the toroid has inner and outer diameters of 10 cm and 14 cm, respectively, and has circular cross-section area, what is the cross-sectional area, in  $cm^2$ , of the presented magnetic circuit? [1 decimal place] [5]

$$r = \frac{D}{2} = \frac{1}{2} \left( \frac{D_2}{2} - \frac{D_1}{2} \right)$$
$$A = \pi r^2 = 12.6 \text{ cm}^2$$
Ans: 12.6 cm<sup>2</sup>

12. A toroid made of steel of relative permeability of 1800 is wound with a coil of 100-turns, carrying a current of 1 A dc. What is the value of the mmf, in A, produced by the current-excited coil? [A whole number, 0 decimal places] [5]

$$F = NI = 100 \text{ A}$$
  
Ans: 100 A

13. A toroid made of steel of relative permeability of 1800 is wound with a coil of 100-turns, carrying a current of 1 A dc. What is the magnetic field intensity, in A/m, in the middle of the cross-section of the toroid? [A whole number, 0 decimal places] [7.5]

$$H = \frac{F}{l} = \frac{NI}{l_{mean}} = 265 \text{ A}$$

14. A toroid made of steel of relative permeability of 1800 is wound with a coil of 100-turns, carrying a current of 1 A dc. What is the magnetic flux desnsity, in T, in the middle of the cross-section of the toroid? [1 decimal place] [7.5]

$$B = \mu H = \mu_r \mu_0 H = 0.6 \text{ T}$$

15. A toroid made of steel of relative permeability of 1800 is wound with a coil of 100-turns, carrying a current of 1 A dc. If the crossectional area of the magnetic circuit is  $10 \text{ cm}^2$ , what is the total stored energy, in mJ, in the toroid? [1 decimal place] [7.5]

$$W = \frac{1}{2}BH \times vol = \frac{1}{\mu_r \mu_0}B^2 Al = 0.0377 \text{ J}$$
  
Ans: 37.7 mJ

A Zulu 10/07/2021