



The University of Zambia
School of Engineering
Department of Civil and Environmental Engineering
CEE 3211 – Mechanics of Materials Test (2024)

Instructions

Attempts all four questions. All Questions Carry equal marks

Duration: 2 hours

Q1. The assembly consists of two 25-mm-diameter steel ($E_s = 200$ GPa) rods (AB and CD), a 35-mm-diameter aluminium ($E_{al} = 70$ GPa) rod EF, and a rigid bar AEC. With the loads applied as shown, determine the **overall displacement** of end **F** of rod EF.

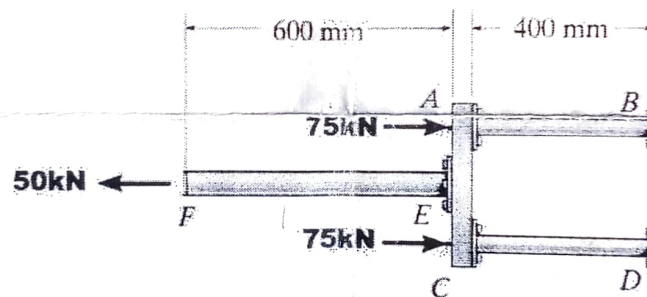


Fig Q1

Q2 A composite cylindrical rod, ABCD consists of bar 1, Steel ($E = 207$ GPa) and Bar 2, Brass ($E = 101$ GPa) fixed at both ends as shown in Figure Q2. The member has a gap of 4mm as shown. The thermal coefficient of expansion for steel and brass coefficient as $11.7 \times 10^{-6}/^{\circ}\text{C}$ and $18 \times 10^{-6}/^{\circ}\text{C}$ respectively. The composite rod is subjected to a temperature rise of 130°C . Assuming the rod is initially unstressed: Take length $AB=600\text{mm}$ and $CD = 900\text{mm}$. Area for steel and brass are 275mm^2 and 390mm^2 .

- a. Calculate the **stress induced** in both bars AB and CD

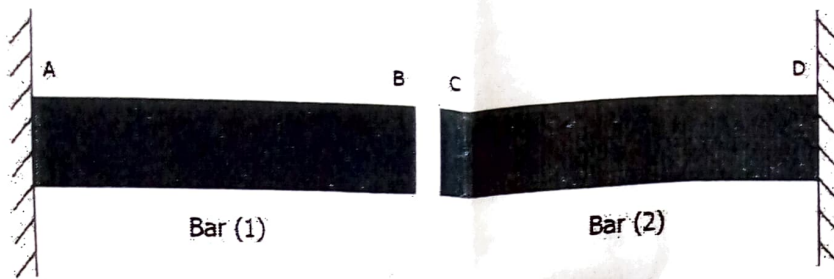


Fig Q2

Q3 A steel beam of 6m in length has a channel cross-section shown in Figure Q3 with two-point loads.

- Draw the shear and moment diagrams
- Calculate the **maximum compressive** and **tensile** stresses. Take E_{st} as 200 GPa.

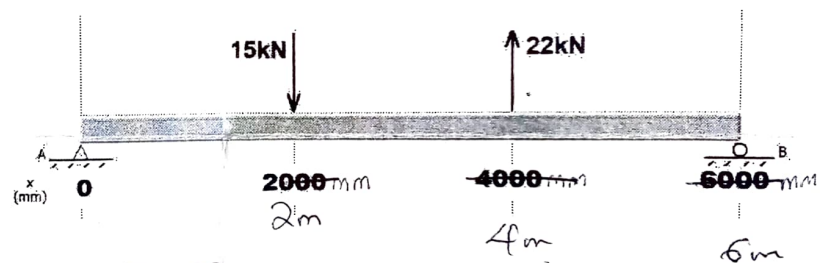
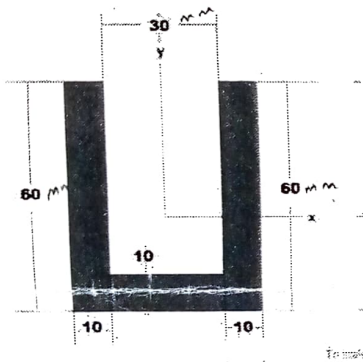


Fig. Q3

Q4. A shaft shown in Figure Q4 has shaft 1 made of solid steel ($G = 76$ GPa) and Titanium ($G = 45$ GPa) shaft (2). Shaft 1 has a length of 100mm, and a diameter of 50mm, while shaft 2 has a length of 130mm and a diameter of 30mm.

If an external torque $T_B = 800$ N.m is applied at point B as shown, calculate the torque T_C required at point C so that the rotation angle of point C relative to A is **zero**.

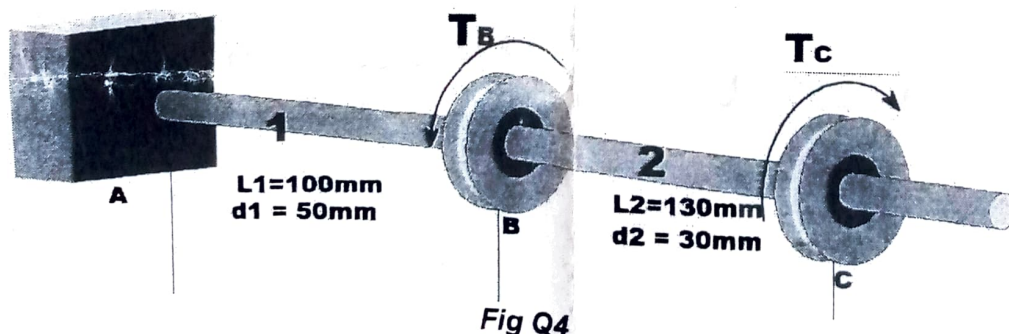


Fig Q4

THE UNIVERSITY OF ZAMBIA

SCHOOL OF ENGINEERING

DEPT. CIVIL & ENVIRONMENTAL ENGINEERING

CEE 3211

MECHANICS OF MATERIALS

[TEST SOLUTIONS]

2024

Q1.

$$P_{EF} = 50 \times 10^3 \text{ N (Tension)}$$

$$P_{AB/CD} = \frac{50 \text{ kN} - 75 \text{ kN}}{2}$$

$$= 25 \text{ kN} - 75 \text{ kN}$$

$$= -50 \text{ kN}$$

$$= -50 \times 10^3 \text{ N (Compression)}$$

DataSteel (AB & CD)

$$D = 25 \text{ mm}$$

$$E = 200 \times 10^3$$

Aluminium (EF)

$$D = 35 \text{ mm}$$

$$E = 70 \times 10^3$$

$$\delta_T = \delta_{EF} + \delta_{AB}$$

$$\delta_T = \frac{P_{EF} L}{AE_{EF}} + \frac{P_{AB} L}{AE_{AB}}$$

$$\delta_T = \frac{(50 \times 10^3 \text{ N}) \times (600 \text{ mm}) \times 4}{[\pi \cdot (35)^2] \times [70 \times 10^3]} + \frac{(-50 \times 10^3 \text{ N}) \times (400) \times 4}{[\pi \cdot (25)^2] \times [200 \times 10^3]}$$

$$\delta_T = \frac{60 \times 10^6 \times 2}{269,391,570} - \frac{40 \times 10^6 \times 2}{392,699,081.7}$$

$$\delta_T = \frac{120 \times 10^6}{269,391,570} - \frac{80 \times 10^6}{392,699,081.7}$$

$$\delta_T = 0.445448237 \text{ mm} - 0.203718327 \text{ mm}$$

$$\delta_T = 0.241729909 \text{ mm}$$

$$\therefore \delta_T = 0.242 \text{ mm}$$

22. $\delta_{\text{due to } \Delta T} = \delta_{AB} + \delta_{CD}$

$$\delta = \alpha \Delta T L + \alpha \Delta T L$$

$$\delta = \alpha \Delta T L + \alpha \Delta T L$$

$$\delta = (11.7 \times 10^{-6} \times 130 \times 600) + (18 \times 10^{-6} \times 130 \times 900)$$

$$\delta = 0.9126 \text{ mm} + 2.106 \text{ mm}$$

$$\delta = 3.0186 \text{ mm}$$

Since $(\delta_{\text{due to temp}})$ is less than 4 mm, then there won't be any stress induced in the bars.

Data
Bar 1 (Steel) AB

$$E = 207 \times 10^3$$

$$\alpha = 11.7 \times 10^{-6}$$

$$L_{AB} = 600 \text{ mm}$$

$$A_{AB} = 275 \text{ mm}^2$$

Bar 2 (Brass) CD

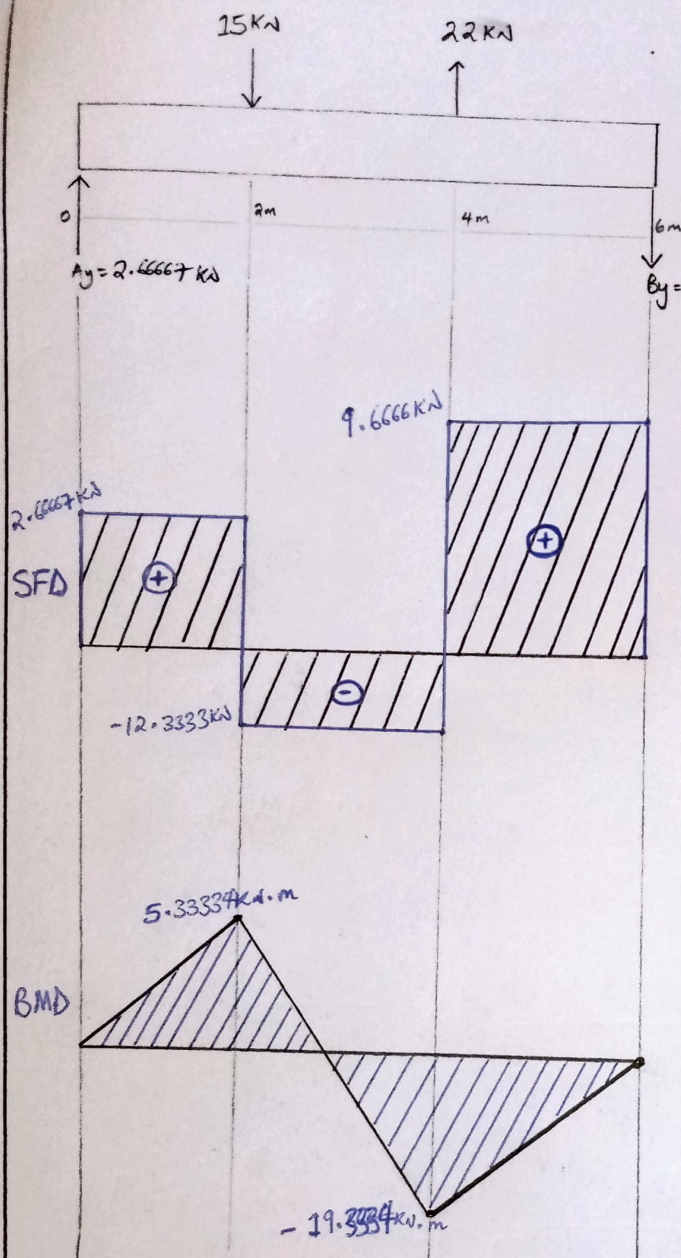
$$E = 101 \times 10^3$$

$$\alpha = 18 \times 10^{-6}$$

$$L_{CD} = 900 \text{ mm}$$

$$A_{CD} = 390 \text{ mm}^2$$

Q3.



$$\uparrow \sum M_A = -15(2) + 22(4) - B_y(6) = 0$$

$$= -30 + 88 - B_y = 0$$

$$-B_y(6) = -58$$

$$-B_y(6) = -58$$

$$B_y = 9.6667 \text{ kN}$$

$$+\uparrow \sum F_y = A_y + 22 \text{ kN} - 15 \text{ kN} - B_y = 0$$

$$A_y + 22 \text{ kN} - 15 \text{ kN} - 9.6667 \text{ kN} = 0$$

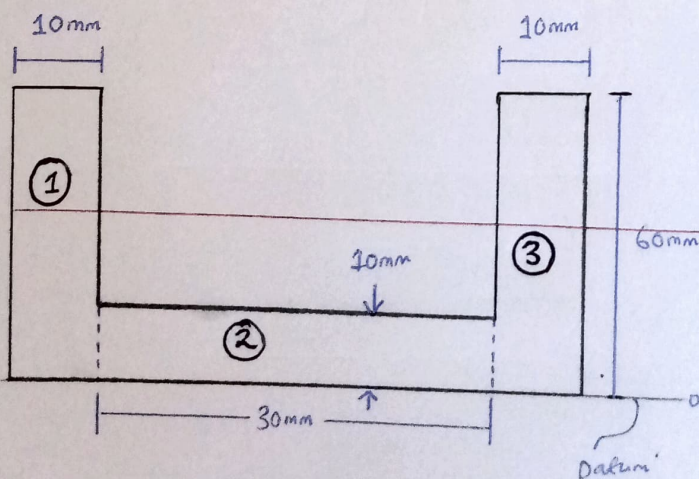
$$A_y - 2.6667 \text{ kN} = 0$$

$$A_y = 2.6667 \text{ kN}$$

$$\text{Maximum Bending moment} = -19.3334 \text{ kN}\cdot\text{m}$$

$$= -19.3334 \text{ kN}\cdot\text{m}$$

$$= -19,333,400 \text{ N}\cdot\text{mm}$$



$$\bar{y} = \frac{\sum A\bar{y}}{\sum A}$$

	A	$\bar{y}$	$A\bar{y}$
1	600 mm	30 mm	18,000 mm
2	300 mm	5 mm	1,500 mm
3	600 mm	30 mm	18,000 mm
Σ	1,500 mm		37,500 mm

$$\bar{y}_{c.s} = \frac{37,500 \text{ mm}}{1,500 \text{ mm}}$$

$$\bar{y}_{c.s} = 25 \text{ mm}$$

$$I = I_1 + I_2 + I_3$$

$$I_1 = \frac{1}{12} b h^3 + A d^2$$

$$I_1 = \frac{1}{12} \times (10)(60)^3 + (60 \times 10)(5)^2$$

$$I_1 = \frac{1}{12} (10 \times 60^3) + (60 \times 10)(5)^2$$

$$I_1 = 180,000 + 15,000$$

$$I_1 = 195,000 \text{ mm}^4$$

$$\underline{I_2}$$

$$I_2 = \frac{1}{12} b h^3 + A d^2$$

$$I_2 = \frac{1}{12} (30 \times 10^3) + (30 \times 10)(20)^2$$

$$I_2 = 2,500 + 120,000$$

$$I_2 = 122,500 \text{ mm}^4$$

$$\underline{I_3}$$

$$I_3 = \frac{1}{12} \times (10)(60)^3 + (60 \times 10)(5)^2$$

$$I_3 = 180,000 + 15,000$$

$$I_3 = 195,000 \text{ mm}^4$$

$$I = I_1 + I_2 + I_3$$

$$I = 195,000 \text{ mm}^4 + 122,500 \text{ mm}^4 + 195,000 \text{ mm}^4$$

$$I = 512,500 \text{ mm}^4$$

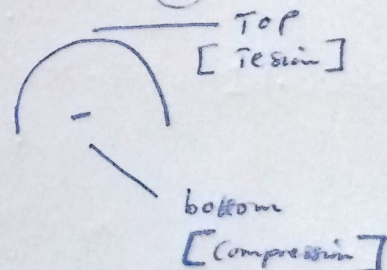
$$\sigma_{\text{top}} = \frac{M c}{I}$$

$$\sigma_{\text{top}} = \frac{19,333,400 \text{ N} \cdot \text{mm} \times 35 \text{ mm}}{512,500 \text{ mm}^4}$$

$$\sigma_{\text{top}} = 1320.329756 \text{ MPa}$$

$$\sigma_{\text{maximum Tensile}} = \underline{\underline{1320.33 \text{ MPa (T)}}}$$

negative Bending moment



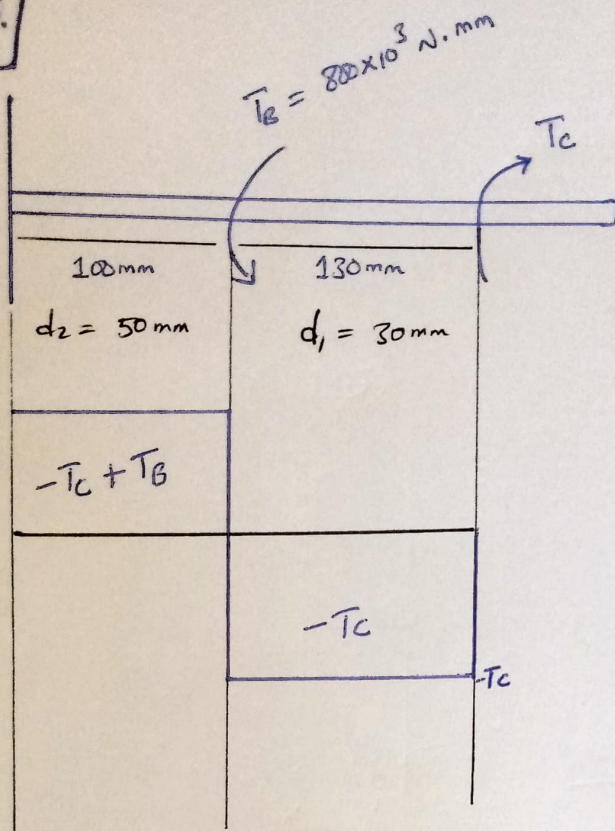
$$\sigma_{\text{bottom}} = \frac{M c}{I}$$

$$= \frac{19,333,400 \text{ N} \cdot \text{mm} \times 25 \text{ mm}}{512,500 \text{ mm}^4}$$

$$\sigma_{\text{bottom}} = 943.0926829$$

$$\sigma_{\text{maximum Compression}} = \underline{\underline{943.09 \text{ MPa (C)}}}$$

[Q4.]



Data

Shaft 1 (Steel)

$$L_1 = 100 \text{ mm}$$

$$d_1 = 50 \text{ mm}$$

$$G = 76 \times 10^3$$

Shaft 2 (Brass)

$$L_2 = 130 \text{ mm}$$

$$d_2 = 30 \text{ mm}$$

$$G = 45 \times 10^3$$

$$\phi = \frac{TL}{JG}$$

$$\phi_A = \phi_C + \phi_B$$

$$0 = \frac{T_C L}{JG} + \frac{T_B L}{JG}$$

$$0 = \frac{-T_C L}{JG} + \frac{(-T_C + T_B) L}{JG}$$

$$0 = \frac{-T_C \cdot 130 \times 32}{\pi \cdot (30)^4 \times (45 \times 10^3)} + \frac{(-T_C + T_B) \cdot 100 \times 32}{\pi \cdot (50)^4 \times (76 \times 10^3)}$$

$$0 = \frac{-T_C 4160}{1.145110522 \times 10^{11}} + \frac{-T_C 3200}{1.49225651 \times 10^{12}} + \frac{2,560 \times 10^6}{1.49225651 \times 10^{12}}$$

$$0 = -T_C 3.63 \times 10^{-8} - T_C 2.1444 \times 10^{-9} + 1.71552 \times 10^{-3}$$

$$\frac{-1.71552 \times 10^{-3}}{-3.8444 \times 10^{-8}} = \frac{-T_C 3.8444 \times 10^{-8}}{-3.8444 \times 10^{-8}}$$

$$T_C = 44,591.59 \text{ N}\cdot\text{mm}$$

$$\therefore T_C = 44,591.60 \text{ N}\cdot\text{mm}$$